

Thematic Program on

Rational Points, Algebraic Cycles and the Local-Global Principle

January 2026 - May 2026

Variants of the local-global principle beginning with Hasse's theorem for quadratic forms are many. Extension of Hasse's theorem to homogeneous spaces of connected linear algebraic groups over a number field, and to homogeneous spaces of linear algebraic groups over function fields in one variable over a local field are two such variants. Conjectures concerning the existence of rational points and zero-cycles, and their interactions with analytic number theory and motivic cohomology fall under the realm of this study. Involving objects like Brauer group and Chow groups, and drawing techniques from algebraic K-theory, this program sets out to examine recent progress in these areas.

$$\begin{aligned} \text{Ker } [\mathbb{H}^1(K, G) \rightarrow \prod_{v \in \Omega} \mathbb{H}^1(K_v, G)] \\ \overline{X(k)^{\text{top}}} \subset X(\mathbb{A}_k)^{\text{Br}} \\ \varprojlim_n \text{CH}_0(X)/n \rightarrow \prod_{v \in \Omega} \varprojlim_n \text{CH}_0(X_v)/n \rightarrow \text{Hom}(\text{Br}(X), \mathbb{Q}/\mathbb{Z}) \\ \text{CH}^i(\mathbf{X}/\mathbb{F}) \otimes \mathbb{Z}_\ell \rightarrow \mathbb{H}_{\text{ét}}^{2i}(\mathbf{X}, \mathbb{Z}_\ell(i)) \end{aligned}$$

Organisers:

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Program Calendar:

- **Algebraic Cycles: 1 January - 15 February**
Workshop: Arithmetic of Algebraic Cycles, 27 - 29 January
- **Algebraic Groups: 10 February - 20 March**
Workshop: Linear Algebraic Groups over Arithmetic Fields, 17 - 19 March
- **Rational Points: 15 March - 30 April**
Workshop: Varieties with many rational points, 14 - 16 April

